

# Water-resource use and conflict in a two-sector evolutionary model

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# Overview

- \* Over the last few years the growing problems of water scarcity and water pollution have attracted increasing attention
- \* Water conflicts/competition both across countries (e.g. Chad-Nigeria-Camerun, Israel vs. Jordan, Siria vs. Turkey etc...) and within countries (among competing populations/firms/sectors)
- \* To deal with these problems the introduction of a system of market incentives (and disincentives) in water management has been proposed

## Water tradable permits: applications

- \* Water tradable pollution rights (WTPR): mainly US (Colorado, California, Wisconsin etc...) and Australia (Murray-Darling basin)
- \* Water tradable abstraction rights (WTAR): US, Australia but also Chile, Mexico and other LDCs
- \* Mixed results: some experiences very successful (e.g. Murray-Darling basin, Idaho, California), others unsuccessful (small number transactions in Wisconsin, Colorado...)

# Related Literature

- Huge literature on ETS (mainly on GHG emission trading)
- Vast literature on water applications (mainly case studies): Borghesi (2013, JEPM), Fisher-Vanden and Olmstead (2013, JEP) for surveys on WTPR and WTAR
- Recent empirical studies on invention and diffusion of water supply and water efficiency technologies (Conway et al., 2015)
- Small subset of theoretical models on water trading (mainly simulations)
- This paper: Study consequences of a market for water-use permits in the presence of a population of interacting economic agents characterized by imitative behaviours

# Aim of the paper

- \* investigate the theoretical framework underlying the application of water tradable permits by proposing a dynamic evolutionary model to capture: (i) water competition among sectors and (ii) bounded rationality among economic agents
- \* Two-sector model with replicator dynamics
  - Antoci, Borghesi, Sodini, 2014. "ETS and technological innovation: a random matching model", Handbook Climate Change, Oxford University Press
  - Antoci, Borghesi, Russu, Ticci, 2015: 2-sector model on FDI (Ecol Econ)

# A TWO-SECTOR MODEL

- \* 2 sectors: A and B
- \* Population of agents
- \* The size of the population is constant and represented by the positive parameter  $N$
- \* the variable  $x(t)$  indicates the share of the population working in sector A at time  $t$  (so  $1 \geq x(t) \geq 0$ , and  $1-x(t)$  indicates the share of the population working in sector B)
- \* The production activities in both sectors depend on the stock  $W_i$  ( $i=A,B$ ) of available water resources ( $W_i$  can also be interpreted as an index that takes water "quality" into account)

# SET UP OF THE MODEL

- \*  $W_A(x) = \bar{W}_A - \alpha x \bar{N} - \beta(1-x)\bar{N}$  where:  $\alpha > \beta > 0$
- \*  $W_B(x) = \bar{W}_B - \gamma x \bar{N} - \delta(1-x)\bar{N}$  where:  $\gamma > \delta > 0$
- \*  $\pi_i[W_i(x)]$ : payoff of an agent working in  $i=A,B$
- \*  $\pi'_i[\cdot] > 0$ : payoffs strictly increasing functions of available water resources
- \* 2 possible cases:  $\pi_A[W_A(x)]$  decreases more or less rapidly than  $\pi_B[W_B(x)]$  as  $x$  increases.
- \* Pricing mechanism: water either free ( $p=0$ ) or priced as follows:
  - \*  $p = \bar{p} + \mu x \bar{N}$  where:  $\bar{p} \geq 0, \mu \geq 0$

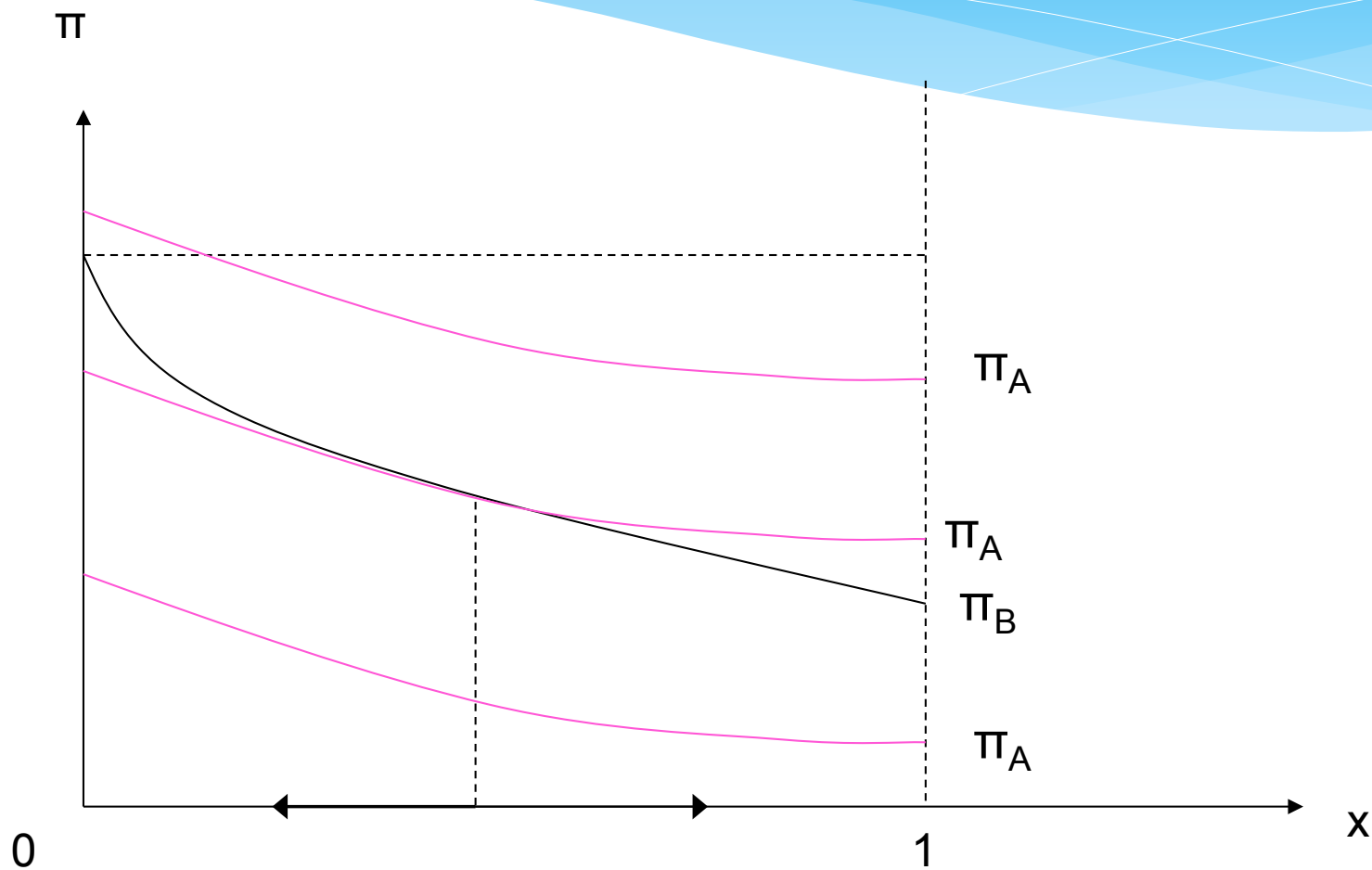
# Replicator dynamics

(Weibull, 1995)

- \*  $\dot{x} = x(1 - x)\{\pi_A[W_A(x)] - \pi_B[W_B(x)]\}$
- \* Agents move towards the most profitable sector (i.e. that has the highest payoff)
- \* Possible steady states:
  - \* Extreme equilibria:  $x=0, x=1$
  - \* Inner equilibrium:  $0 < x < 1$  s.t.  $\pi_A[W_A(x)] = \pi_B[W_B(x)]$



# Scenario 1: payoff in A decreases less rapidly than in B



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## \* 3 possible sub-cases:

\* 1.1)  $\pi_A(x)$  always above  $\pi_B(x) \rightarrow x=1$  (full specialization in A)

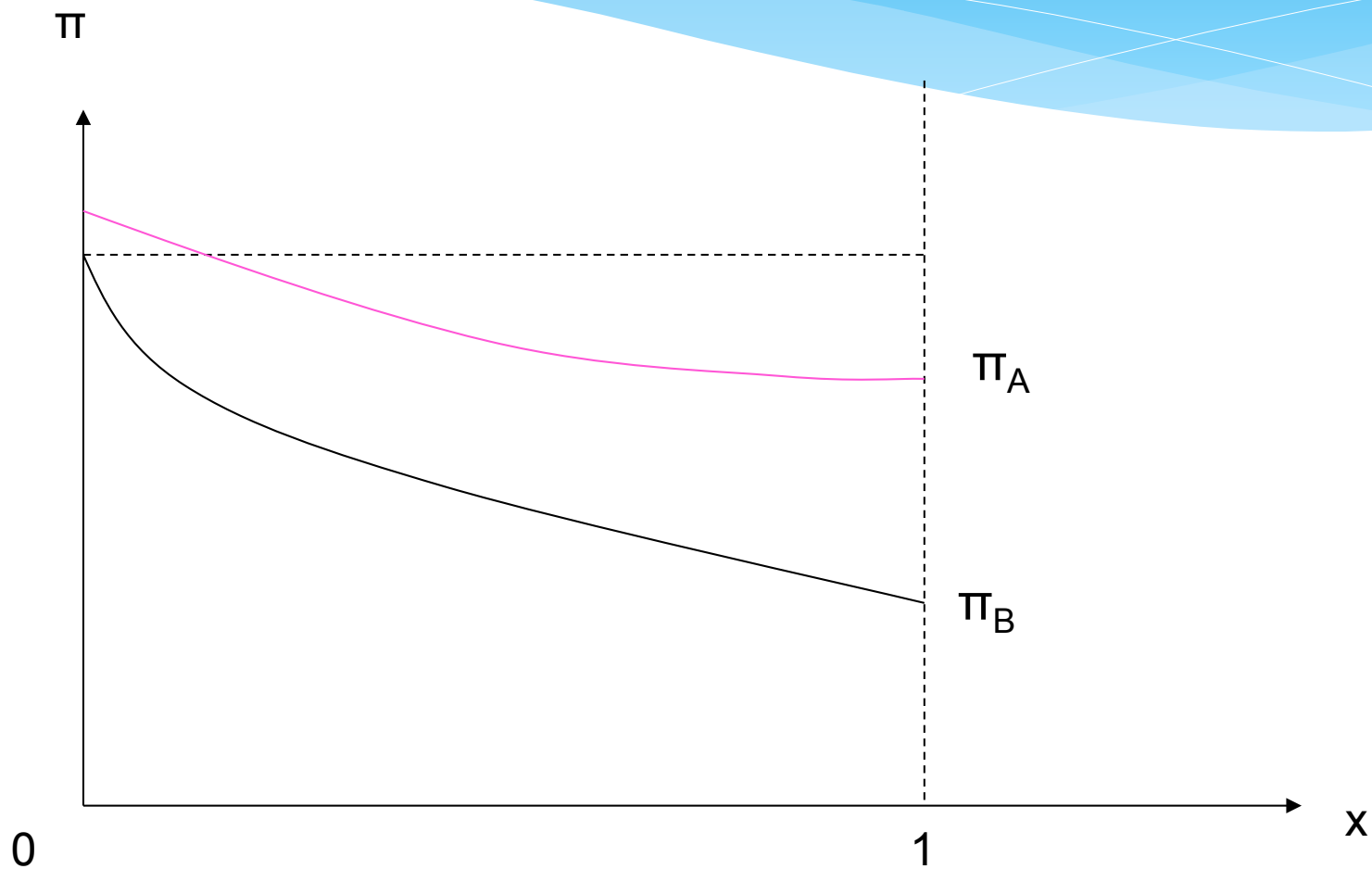
\* 1.2)  $\pi_A(x)$  always below  $\pi_B(x) \rightarrow x=0$  (full specialization in B)

\* 1.3) Curves  $\pi_A(x)$  and  $\pi_B(x)$  cross in the  $(x,\pi)$  plane at some  $x^* \in (0,1)$

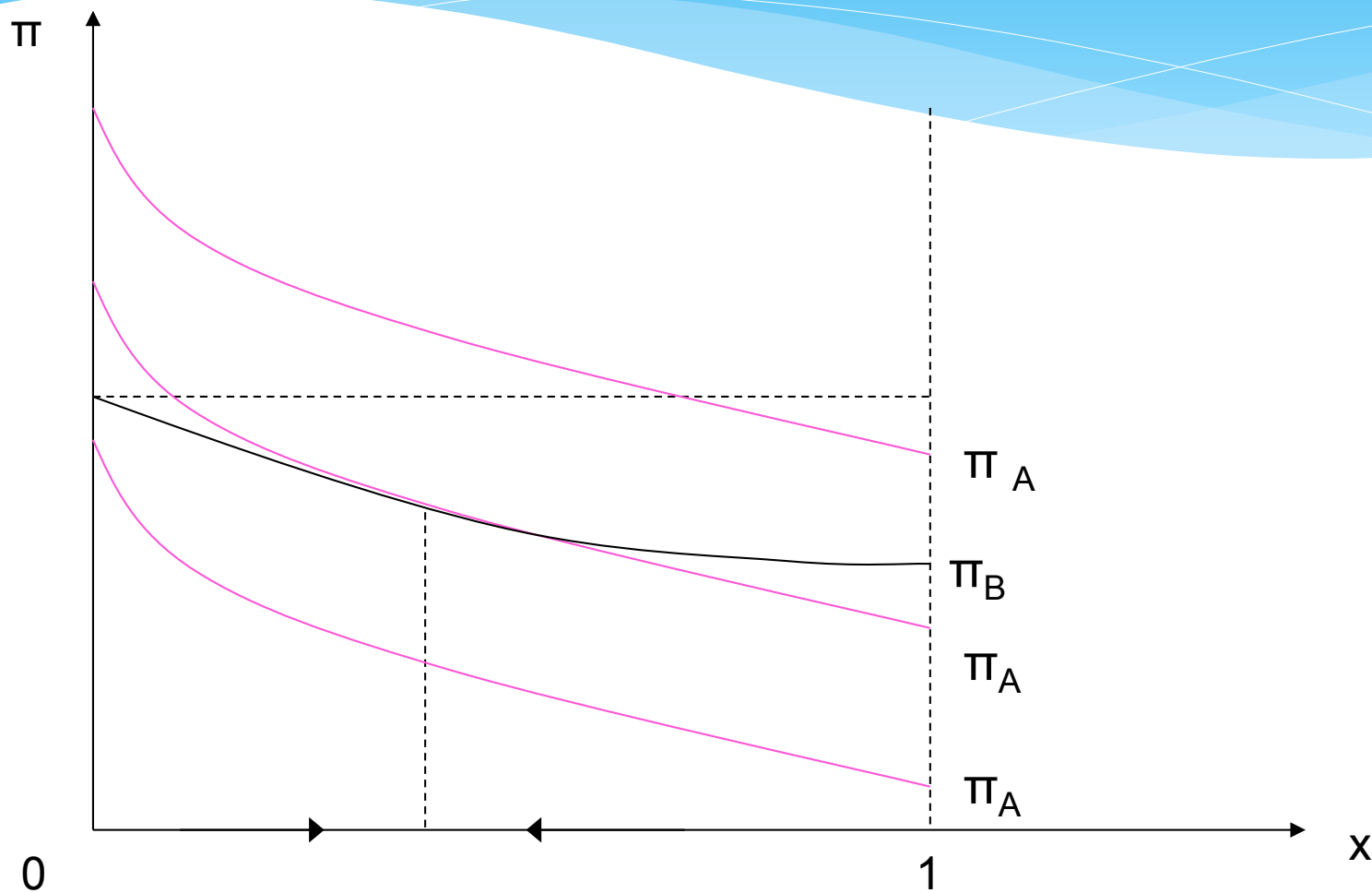
$\rightarrow$  “bistable dynamics”: if the initial share  $x$  of agents working in A is below the threshold level, then all agents will work in B at the end of the day; vice-versa, if is larger than the threshold level (path-dependency)

If  $\pi_B(0) > \pi_A(1)$ , the individually rational choice of moving to A produces a socially undesirable equilibrium at the aggregate level for the community as a whole  $\rightarrow$  Pareto-dominated stable Nash equilibrium

# Scenario 1: payoff in A decreases less rapidly than in B



# Scenario 2: payoff in A decreases more rapidly than in B



## Scenario 2: payoff in A decreases more rapidly than in B

- \* 3 possible sub-cases:

- \* 2.1)  $\pi_A(x)$  steeper than  $\pi_B(x)$  but it always remains above it  $\rightarrow x=1$

- \* 2.2)  $\pi_A(x)$  steeper than  $\pi_B(x)$  and lies always below it  $\rightarrow x=0$

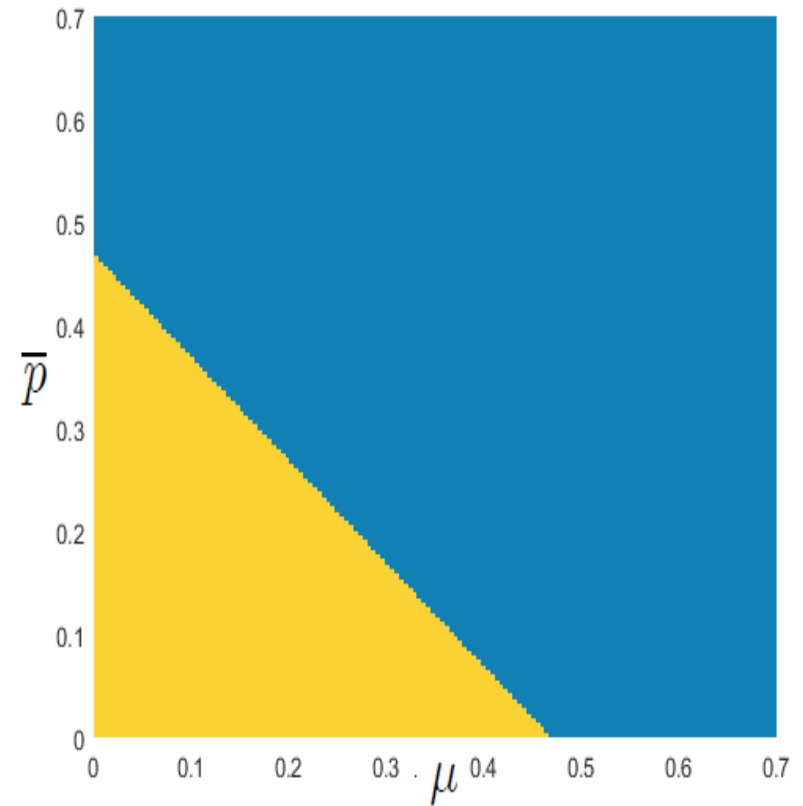
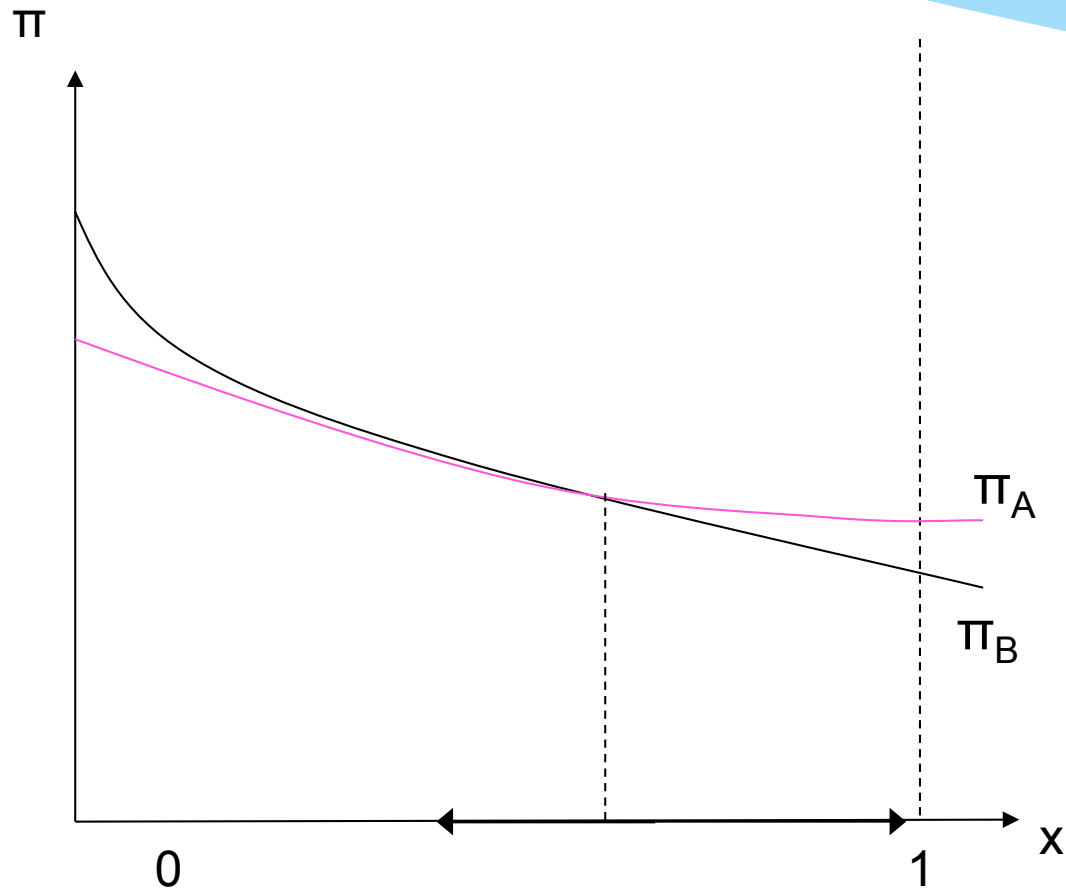
- \* 2.3)  $\pi_A(x)$  steeper than  $\pi_B(x)$  and curves cross in the  $(x, \pi)$  plane  $\rightarrow$  converge towards **the stable Nash equilibrium**  $x^* \in (0,1)$

$\pi_B(0) > \pi_i(x^*)$ : although everyone would be better-off working in the lower-impact sector B, the dynamics that emerge from the strategy adoption process leads away from  $x=0$  towards the stable equilibrium  $x^*$ , so that when  $x < x^*$  **the community moves along a Pareto-dominated path.**

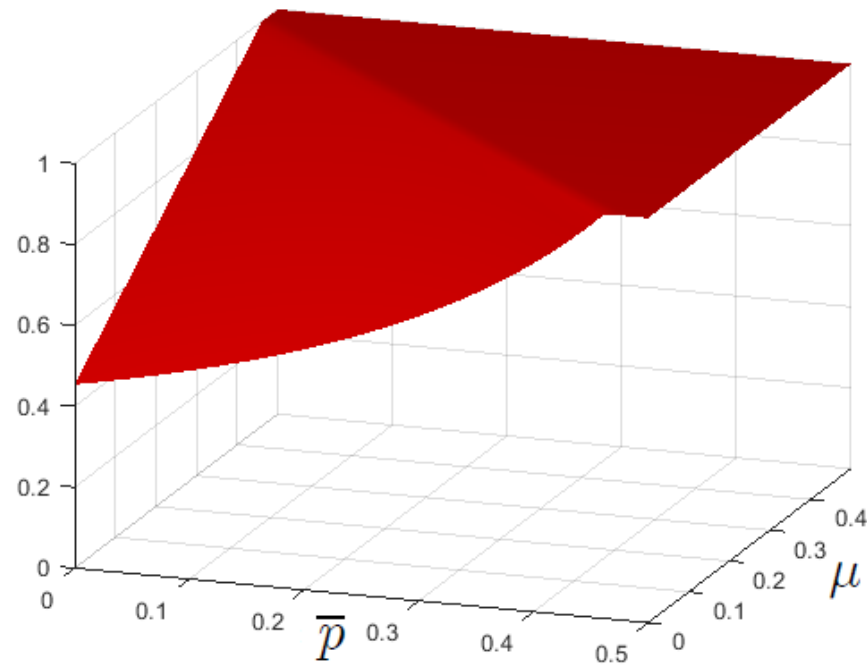
# Pricing water

- \*  $p = \bar{p} + \mu x \bar{N}$  where  $\bar{p} \geq 0, \bar{N} \geq 0$
- \*  $\mu$  = elasticity of water price to demand (e.g. WTP)
- \*  $\bar{p}$  = lower bound (e.g. price floor in an ETS)
- \* By properly modifying  $\bar{p}$  and  $\mu$  the Public Authority can affect the relative position of the curves and the dynamics of the system (and thus avoid Pareto-dominated outcomes)
- \* Fix  $\bar{p}$  and  $\mu$  so as to ensure that the curve  $\pi_A$  lies always below  $\pi_B$ :
- \*  $\pi_A(W_A(x)) - \bar{p} + \mu x \bar{N} < \pi_B(W_A(x))$
- \* Results can hold as long as  $p_A > p_B$

# Simulation results-1: from bistability (yellow) to unique equilibrium $x=0$ (blue)



# Simulation results-2: the separating threshold





# Concluding remarks

- \* Water crucial for production processes but limited → water conflicts/competition among individuals, sectors, countries...
- \* The present paper examines a 2-sector model of water competition with imitative behaviours across agents
- \* If water is unpriced, the society as a whole may end up in a “poverty trap”: individually rational choices lead to full/partial specialization in the most water-consuming (polluting) sector, but agents would be better-off by working in the alternative (“cleaner”) sector.
- \* Water pricing mechanism to “escape” the poverty trap
- \* A properly designed WTAR (WTPR) [e.g. a sufficiently high price floor] can drive the economy away from the Pareto-dominated equilibrium

# Agenda for the future

1. Introduce Leontieff production functions: e.g.  
 $YA = \min[aWA, b \times N]$
2. Intertemporal evolution of water resources (e.g. role of infrastructures such as dams, canalizations etc...) → from unidimensional to bidimensional dynamics (Phase plan in  $x$  and  $W$ )
3. Extend water competition from within countries to across countries



Thank you for your attention!!

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